# Design Optimization and Comparison of Direct-drive Outer-rotor SRMs Based on Fast Current Profile Estimation and Transient FEA

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Abstract—Outer-rotor switched reluctance machines (SRMs) have drawn much attention as promising candidates for in-wheel direct-drive motors of future electric vehicles. This paper presents a systematic performance comparison of three outer-rotor SRM topologies for in-wheel traction applications in terms of the specific torque, electromagnetic efficiency, torque ripple, radial force and mechanical aspects. A generalized design optimization framework for SRMs is proposed to enable the fast evaluation of large numbers of designs generated from the differential evolution (DE) by incorporating an analytical current profile estimation into the transient finite element analysis (FEA). The relationship between the saliency ratio and converter volt-ampere (VA) rating is also discussed. The calculations are then benchmarked with the experimental results from an existing prototype. The effectiveness of the performance prediction method and the proposed optimization approach is validated.

*Index Terms*—Converter VA rating, current profile, differential evolution, direct-drive, in-wheel motor, optimization, segmented rotor, switched reluctance machine.

#### NOMENCLATURE

Inner and outer diameter of rotor, respec-
lively. Shaft diamatar
Thickness of rotor and stator tooth tip,
respectively.
Rotor and stator yoke thickness, respec-
tively.
Angular position of rotor.
Turn-on and turn-off angle in electrical
degrees, respectively.
Rising and falling time represented by
electrical degrees, respectively.
Rotor and stator tooth arc, respectively.
Rotor and stator tooth tip arc, respectively.
Rated phase current (peak value) and phase
current, respectively.
Ratio of stator voke thickness to stator
outer radius.
Ratio of rotor voke thickness to rotor thick-
ness in radial direction.
Ratio of rotor pole arc at rotor inner diam-
*
eter to rotor pole pitch.
eter to rotor pole pitch. Ratio of real rotor tooth arc and real stator
eter to rotor pole pitch. Ratio of real rotor tooth arc and real stator tooth arc to their maximum values, respec-

$k_{rtt}, k_{stt}$	Ratio of real rotor tooth tip arc and real sta-
	tor tooth tip arc to their maximum values,
	respectively.
$k_s$	Split ratio, i.e., ratio of rotor inner diameter
	to rotor outer diameter.
$k_{s1}, k_{s2}$	Ratio of stator main tooth width and stator
	auxiliary tooth width to stator pole pitch,
	respectively.
$k_{spa}$	Ratio of stator pole arc to stator pole pitch.
$k_{sy}$	Ratio of stator yoke thickness to stator
	thickness in radial direction.
$k_{tip1}, k_{tip2}$	Ratio of stator main tooth tip depth and
	stator auxiliary tooth tip depth to stator
	outer radius, respectively.
$k_{wtip1}, k_{wtip2}$	Ratio of stator main tooth tip width and
	stator auxiliary tooth tip width to stator
	pole pitch, respectively.
L, R	Phase inductance and resistance.
$L_a, L_u$	Aligned and unaligned inductance, respec-
	tively.
m	Number of phase.
$N_r, N_s$	Number of rotor poles and stator teeth,
	respectively.
V	Terminal voltage.
$V_{dc}$	Dc bus voltage.
ω	Angular speed of rotor.

## I. INTRODUCTION

Switched reluctance machines (SRMs) are attractive candidates for traction motors of future electric and hybrid vehicles, owing to the rugged construction, relatively high specific torque and efficiency, and inherent fault-tolerant capability [1–3]. The emerging in-wheel direct-drive technology in the automobile industry may further open up new opportunities for SRMs considering their robustness to harsh operational conditions [4].

Outer-rotor configurations are more appealing for in-wheel traction applications, because they facilitate direct coupling to the wheel rim thereby simplifying mechanical transmission. In addition, the increased torque capability due to a higher airgap diameter, and larger rotor inertia, help to dampen the torque ripple and provide smooth and stable operation, even at low speeds.

The design optimization of SRMs is challenging. The evaluation of each design involves intensive computation consid-

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To simplify the optimization problem and to reduce the computation time, analytical magnetic equivalent circuit models or surrogate models were commonly used [6, 7]. Optimizing the static torque instead of the more desired average torque was also adopted to accelerate the optimization process [8, 9].

Most of the existing work on design optimization of SRMs focuses on design space reduction by decreasing the number of design variables. For instance, a conventional 12-slot 8-pole (12s8p) SRM was designed to achieve a predefined torquespeed envelope for electric vehicles and compared with interior permanent magnet and induction motors [10]. In another work, three design variables, i.e., the number of turns, turn-on and turn-off angles were considered, but only the turn-on and turn-off angles were optimized using multiobjective genetic algorithm to maximize the average torque and minimize the torque ripple for each specific design [11]. The design of experiments method and sensitivity analysis were applied to the design optimization of SRMs to identify the less significant variables and narrow down the search space [7, 12].

Reducing the number of independent variables can significantly reduce the computational burden but it is not always possible. When all the design variables have significant impacts on the objective functions, it becomes necessary to reduce the computation time of each FEA evaluation. In order to minimize the computation time for each design, the required current excitation for solving the magnetic field is determined prior to the transient FEA. An inductance approximation method based on Fourier series and magnetostatic FEA was used to construct the current profile and optimize the torque waveform for a 6-slot 4-pole SRM [13], yet the magnetic saturation was not considered. An 80-kW segmented rotor SRM was optimized based on a combination of magnetostatic and transient FEA, where the current excitation profile was estimated from the peak static torque by introducing a few empirical coefficients, which reduces its universality [14].

The multiobjective optimization and electromagnetic performance comparison of three typical outer-rotor SRM topologies have been presented in [15] based on simplified trapezoidal current waveforms. This paper enhances the published conference paper by generalizing the proposed design optimization framework to include more accurate current excitation taking into account the influence of the hysteresis current regulation and the magnetic saturation of phase inductance. An analytical current profile estimation method is proposed to reduce the evaluation time per design without reducing the number of independent variables. The aligned and unaligned inductance information obtained from magnetostatic FEA is used to determine the current excitation profile before the transient magnetic field solver is called, which enables the computation acceleration achieve by the time decomposition method (TDM) [16, 17]. In addition, the definition and calculation of volt-ampere (VA) rating and power factor in SRMs are provided to fill the gap in existing literature on the optimal design of SRMs, considering the fact that the specific torque and converter VA rating are conflicting objectives [18].

This paper is organized as follows. Section II reviews the electromagnetic design considerations of SRMs for in-wheel direct-drive applications. Section III presents the proposed design optimization framework based on fast current profile estimation and multiobjective differential evolution (DE) algorithm. The optimization results are reported and discussed in Section IV, followed by the FE and experimental validation detailed in Section V. Section VI concludes the full paper.

## **II. ELECTROMAGNETIC DESIGN CONSIDERATIONS FOR IN-WHEEL SRMS**

The direct-drive designs in this paper are intended for in-wheel electric and hybrid vehicles, and therefore employ external rotor constructions facilitating direct integration into the wheel. The rotor outer diameter  $D_{or}$  and shaft diameter  $D_{sh}$  are constrained by the wheel rim and shaft, respectively. The speed is relatively low, which is determined by the maximum vehicle speed and wheel outer diameter. Based on the available space in a 10 inch wheel, specifications of the design example are determined, as tabulated in Table I.

## A. Available Topologies

Aside from the conventional SRM topologies with tooth wound coils and weak mutual coupling between phases, quite a few topological variations of SRMs have emerged in the past decade, such as those with more rotor poles than stator teeth [19], with magnetically disconnected rotor segments [14, 20], with split stator teeth [21], with segmented stator [22] and the mutually-coupled type [23, 24]. In general, the number of teeth and rotor poles in SRMs are constrained by [25, 26]

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$$LCM(N_r, N) = mN_r,$$

$$\begin{cases}
N = N_s, & \text{without auxiliary teeth,} \\
N = \frac{1}{2}N_s, & \text{with auxiliary teeth,} 
\end{cases}$$
(1)

where LCM is the least common multiple.  $N_s$  and  $N_r$  are the number of stator teeth and rotor poles, respectively. m is the number of phase. Three candidate SRMs are considered for the targeted application, i.e., a 12-slot 26-pole (12s26p) SRM, a 6-slot 10-pole (6s10p) SRM, and a 12s8p SRM, as shown in Fig. 1. The flux lines and flux density maps of the studied machine topologies at unaligned and aligned positions are also included.

Table I: Design Specifications.

Parameters	Value
Rated torque (Nm)	18 at 600rpm
Current density (A/mm <sup>2</sup> )	$\leq 5$
DC bus voltage (V)	200
Shaft diameter/airgap lengh (mm)	20/0.4
Outer diameter/axial length (mm)	$\leq 240/40$



Fig. 1. Flux lines and flux density maps for example designs of the selected outer-rotor SRM topologies at unaligned and aligned positions: (a) 12s26p SRM, (b) 6s10p SRM and,(c) 12s8p SRM. The three SRMs have the same current density  $4A/mm^2$  and same dimensions: total outer diameter of rotor = 232mm, shaft diameter = 20mm, airgap length = 0.4mm and stack length = 40mm.

In the 12s26p SRM, only the alternate stator teeth are wound with concentrated coils. The teeth which are not wound simply serve as returning paths for the flux, and are narrower than the main teeth with coils.

## B. Mode of Operation

SRMs can be operated in the constant torque mode at low speeds with current chopping control, constant power mode at medium speeds with angular position control and the natural mode at high speeds. Current waveforms vary significantly with the modes of operation and typical current waveforms for different modes of operation have been well illustrated in [27]. The current profile has a significant impact on the average torque and torque ripple, depending on the harmonic contents [28]. For in-wheel direct-drive applications, the rotor speed is relatively low and therefore, the current chopping control with fixed turn-on and dwell angles is employed. The block diagram for the closed-loop speed control of SRMs under study is shown in Fig. 2.



Fig. 2. Closed-loop speed control block diagram for SRMs under study.

## III. DESIGN OPTIMIZATION BASED ON CURRENT PROFILE ESTIMATION AND MULTIOBJECTIVE DE

## A. Current Profile Estimation

In order to estimate the current profile, specifically, the rising and falling times, that can be used for the performance evaluation with transient FEA, the inductance information is required. However, the inductance is dependent on the instantaneous winding current and rotor position, as shown by the unaligned and aligned inductances at different current levels of the three selected topologies in Fig. 3.

To simplify the analysis, the inductance at a given current is assumed to vary sinusoidally with the rotor position. In the unsaturated condition, the inductance is a function of the rotor position and independent of the winding current. The current profile can be readily solved from:

$$V = iR + L(i,\theta)\frac{di}{dt} + i\frac{dL(i,\theta)}{d\theta}\omega$$
  
= 
$$\begin{cases} V_{dc}, & \theta_{on} < \theta \le \theta_{on} + \theta_{rise}, \\ -V_{dc}, & \theta_{off} < \theta \le \theta_{off} + \theta_{fall}, \end{cases}$$
(2)

where V is the terminal voltage of phase winding, i the phase current, R the phase resistance, L the phase inductance,  $\theta$  the



Fig. 3. Typical inductance characteristics of SRMs under study at unaligned and aligned positions.



Fig. 4. Schematic diagram for current profile derivation.

rotor position in electrical degrees,  $\omega$  the corresponding rotor angular speed.

With saturation, the inductance waveform in a full electrical cycle is distorted, as shown by the solid green line in Fig. 4. From  $\theta_{on}$  to  $\theta_{off}$ , the inductance can be approximated by that at  $i = I_p$ , i.e., the black dash-dotted line. Between  $\theta_{off}$  and  $\theta_{off} + \theta_{fall}$ , the inductance sees a dramatic change due to the current decrease. The inductance from  $\theta_{off} + \theta_{fall}$  to  $2\pi$  is that at i = 0, i.e., the black dotted line since the current is zero. A simple equivalent inductance denoted by the dashed blue line is used to approximate the inductance profile between  $\theta_{off}$  and  $2\pi$ . The phase inductance can therefore be written as:

$$\begin{split} L(i,\theta) &= A + B\cos\theta, \\ \begin{cases} \frac{L_u + L_a(I_p)}{2} + \frac{L_u - L_a(I_p)}{2}\cos\theta, & \theta_{on} < \theta \le \theta_{off}. \\ \frac{L_u + L_a(i(\theta = \pi))}{2} + \frac{L_u - L_a(i(\theta = \pi))}{2}\cos\theta, & \theta_{off} < \theta \le 2\pi. \end{cases} \end{split}$$

$$\end{split}$$

$$(3)$$

Neglecting the winding resistance and substituting (3) into (2) yields:

$$V = (A + B\cos\theta)\frac{di}{dt} - iB\omega\sin\theta.$$
 (4)

Considering  $t = \theta/\omega$ ,

ł

the voltage equation (4) can be simplified to:

$$\frac{V}{\omega} = (A + B\cos\theta)\frac{di}{d\theta} - iB\sin\theta.$$
 (5)

The current rising and falling profiles can be fitted by quadratic formulas based on the following:

$$\begin{cases} i|_{\theta=\theta_{on}} = 0\\ \frac{di}{d\theta}|_{\theta=\theta_{on}} = \frac{V_{dc}}{A+Bcos\theta_{on}}\\ i|_{\theta=\theta_{on}+\theta_{rise}} = I_{p}\\ \frac{di}{d\theta}|_{\theta=\theta_{on}+\theta_{rise}} = \frac{V_{dc}+BI_{p}sin(\theta_{on}+\theta_{rise})}{A+Bcos(\theta_{on}+\theta_{rise})},\\ \begin{cases} i|_{\theta=\theta_{off}} = I_{p}\\ \frac{di}{d\theta}|_{\theta=\theta_{off}} = \frac{-\frac{V_{dc}}{\omega}+BI_{p}sin\theta_{off}}{A+Bcos\theta_{off}}\\ i|_{\theta=\theta_{off}+\theta_{fall}} = 0\\ \frac{di}{d\theta}|_{\theta=\theta_{off}+\theta_{fall}} = \frac{-\frac{V_{dc}}{A+Bcos(\theta_{off}+\theta_{fall})}. \end{cases}$$
(6)

The rising time, represented by angle  $\theta_{on}$ , is:

$$\theta_{rise} = \frac{2I_p}{\frac{\frac{V_{dc}}{\omega} + BI_p sin(\theta_{on} + \theta_{rise})}{A + Bcos(\theta_{on} + \theta_{rise})} + \frac{\frac{V_{dc}}{A + Bcos\theta_{on}}}{A + Bcos\theta_{on}}}.$$
 (8)

Similarly, the falling time is:

$$\theta_{fall} = \frac{2I_p}{\frac{V_{dc} - BI_p \sin\theta_{off}}{A + B\cos\theta_{off}} + \frac{V_{dc}}{A + B\cos(\theta_{off} + \theta_{fall})}}.$$
 (9)

Once  $\theta_{on}$  and  $\theta_{off}$  are given,  $\theta_{rise}$  and  $\theta_{fall}$  can be determined by (8) and (9) and the current profile corresponding to a specified dc bus voltage can be constructed for each design based on the determination of aligned and unaligned inductances from magnetostatic simulations. The current profile is then stored in a lookup table and used as the excitation for transient FEA. The current profile can be as simple as a trapezoidal waveform or can include more details in the current rising and falling periods.

The proposed current profiling estimation is verified by transient FE calculations with voltage source excitation. Current source 1 employs the simplified trapezoidal current waveform and current source 2 uses a more detailed piece-wise linear current waveform whose slopes at  $\theta_{on}$ ,  $\theta_{on} + \theta_{rise}$ ,  $\theta_{off}$  and  $\theta_{off} + \theta_{fall}$  are the same as those of the real current profile, as shown in Fig. 5.

Current source 2 provides a very good approximation for the accurate current waveform from voltage source excitation in



Fig. 5. FE results using current source and voltage source excitations

general, except at the peak current interval, where the current is chopped to achieve the rated current. Current source 1 produces some deviations in the current falling period, which causes some differences in instantaneous flux linkage, terminal voltage and torque. For simplicity, current source 1 is used in the optimization studies.

It can be seen that  $\theta_{rise}$  is related to the dc bus voltage, rated current, supply frequency and inductance profiles. The 12s26p SRM has the highest unaligned inductance and therefore the longest rising time. A higher dc bus voltage will accelerate the rise of the current, but it also increases the converter VA rating. The converter VA rating used in this paper is defined as the product of the peak current and peak voltage in each switch, considering that the ratio between peak current and rms current is difficult to define and it can vary between wide limits depending on the control strategy and the electromagnetic design of the motor. The rms phase current typically lies between 0.3 and 0.5 times the peak current according to [18].

## B. Optimization Framework

The proposed optimization framework based on the current profile estimation is illustrated in Fig. 6. The current profiles constructed from (8) and (9) for the three selected topologies shown in Fig. 1 are illustrated in Fig. 7. It can be seen that the 12s8p has the shortest rising and falling time among the three SRMs. The 12s26p SRM has the longest rising and falling time due to its large unaligned inductance and small saliency ratio, which is defined as the ratio between the aligned inductance at the rated current and the unaligned inductance.

#### C. Optimization Implementation

The total electromagnetic loss and total active mass are the two objectives considered in this study. All the studied machine designs produce the same target torque of 18Nm at 600r/min, and have the same outer diameter 232mm, airgap length 0.4mm and number of turns per phase 200. The input variables considered in the optimization are geometric parameters, whose ranges and values for the reference designs are tabulated in Table II. The geometric parameters are illustrated in Fig. 8. The ranges for the variables are initially determined by varying values for the reference design by a certain percentage,  $\pm 20\%$ , in this study, and changed iteratively according to the distributions of variables for Pareto front designs. In 12s8p and 6s10p SRMs, 7 independent geometric variables are considered, and the 12s26p SRM has 11 variables.

With the constructed current profiles, two-dimensional (2D) FE models with current source excitations are developed. In addition to the total electromagnetic loss and total active mass, the torque ripple, radial force and mechanical aspects, converter VA rating and saliency ratio are also evaluated. The evaluation of the core losses require at least two electrical cycles, and the TDM within ANSYS Maxwell, which permits the parallel computing of multiple time steps is employed to speed up the calculation [16]. The TDM method can be applied to SRMs and produce the same results compared with the non-TDM as long as the excitation applied to the FE model is independent of the simulation history [17]. As



Fig. 6. Flow chart of the proposed DE-based multiobjective design optimization.



Fig. 7. Current profiles used in the optimization.

the geometric parameters vary over the specified ranges, the electromagnetic torque will change as well. To ensure all the designs produce the same target torque, and have the same thermal performance, the stack length is modified from design to design and the current density in conductors are keep constant at  $4A/mm^2$ .

## IV. OPTIMIZATION RESULTS AND DISCUSSION

## A. Mass and Loss

The optimization results for mass and loss are shown in Fig. 9. The distribution of evaluated designs in the loss-mass plane



Fig. 8. Geometric design variables used in the parametric models for: (a) 12s26p SRM, (b) 6s10p SRM, and (c) 12s8p SRM. Independent variables are shown in black fonts. Those in blue and between parenthesis are constants.

Table II: Independent Design Variables and Their p.u. Ranges.

Design variable	12s26 Range	Ref.	12s8p Range	Ref.	6s10p Range	Ref.
$k_s$	[0.85, 0.92]	0.85	[0.76, 0.85]	0.80	[0.76, 0.85]	0.80
$k_{st}$	_	_	[0.92, 1.00]	0.96	[0.36, 0.54]	0.96
$k_{stt}$	-	_	[0.80, 1.20]	1.00	[0.80, 1.20]	1.00
$k_{sy}$	_	-	[0.45, 0.62]	0.54	[0.45, 0.62]	0.54
$k_{ry}$	_	-	[0.48, 0.72]	0.60	[0.48, 0.72]	0.60
$k_{rt}$	_	-	[0.31, 0.47]	0.39	[0.36, 0.54]	0.45
$k_{rtt}$	-	-	[0.31, 0.47]	0.39	[0.36, 0.54]	0.45
$k_{spa}$	[0.90, 0.95]	0.90	-	-	-	-
$k_{s1}$	[0.18, 0.22]	0.21	-	-	-	-
$k_{s2}$	[0.09, 0.15]	0.13	-	-	-	-
$k_{tip1}$	[0.07, 0.14]	0.10	-	-	-	-
$k_{tip2}$	[0.12, 0.14]	0.12	-	-	-	-
$k_{wtp1}$	[0.04, 0.06]	0.04	-	-	-	-
$k_{wtp2}$	[0.04, 0.07]	0.04	-	-	-	-
$k_{by}$	[0.30, 0.60]	0.32	-	-	-	-
$k_{rpa1}$	[0.70, 0.95]	0.85	-	-	-	-
$k_{rpa2}$	[0.20, 0.50]	0.32	-	_	-	-

shows that in order to produce the target torque, the 12s26p SRM, generally, requires much smaller mass and incurs lower losses. Some of the 6s10p Pareto-front designs can achieve nearly the same minimum loss compared with the 12s26p SRMs, but the total active mass has to be increased. The 12s8p designs have the highest loss and the minimum weight is still about 30% more than the 12s26p counterpart. The lightest designs, which are of more interest to reduce the total unsprung mass of the vehicle, are visualized in Fig. 10, whose details are tabulated in Table III.



Fig. 9. Mass and loss for the studied designs of the three machine topologies. The large star marks the reference prototype design and smaller stars identify the other reference designs. The designs selected for further discussion are marked by squares.



Fig. 10. Cross sections of the selected Pareto-front designs with the lowest total mass. (a) 12s26p M-1, (b) 6s10p M-2, and (c) 12s8p M-3.

The three selected designs have nearly the same converter VA rating. M-1 shows better performance in terms of the specific torque/power and torque ripple. M-2 has the highest electromagnetic efficiency and goodness factor, but the lowest torque density and specific torque due to the large stack length and end coil size. M-3 has the largest torque/power density because of the small end coil but the electromagnetic efficiency is greatly reduced. The 1.5kW prototype was run with a reduced current to produce 18Nm at 600rpm for the purpose of comparison.

## B. Torque ripple

The torque ripple has been included in Fig. 11. Since the torque ripple is not one of the optimization objectives, the torque ripple of Pareto-front designs shows some diversity.

Table III: Performance comparison of the lightest designs identified in Fig. 9 and shown in Fig. 10. The stack length is modified to obtain the target torque 18Nm at 600rpm, and the current density is maintained at 4A/mm<sup>2</sup>.

Design	Prototype	M-1	M-2	M-3
Lamination steel	M27-29G		M19-24G	
Stack length (mm)	40.0	26.3	37.0	30.9
Volume (L)	4.3	3.3	4.0	2.4
Mass of steel (kg)	4.5	4.8	7.2	7.0
Mass of copper (kg)	3.2	2.0	4.0	2.1
Total mass (kg)	7.7	6.8	11.2	9.1
Core loss (W)	31.3	36.4	41.2	31.2
Copper loss (W)	117.3	165.6	136.8	324.0
EM efficiency (%)	88.3	84.8	86.4	76.1
Converter VA rating (kVA)	4.3	3.9	3.9	4.1
Torque ripple (%)	51.4	19.4	48.3	77.4
Torque density (Nm/L)	4.2	5.5	4.5	7.5
Power density (kW/L)	0.26	0.34	0.28	0.47
Specific torque (Nm/kg)	2.3	2.6	1.6	2.0
Specific power (kW/kg)	0.14	0.16	0.1	0.12
Goodness factor (Nm/ $\sqrt{W}$ )	1.48	1.27	1.35	0.96



Fig. 11. The variation of mass versus loss together with torque ripple indicated on a color scale for: (a) 12s26p SRM, (b) 6s10p SRM, and (c) 12s8p SRM.

Most of the Pareto-front designs of 12s26p SRM have relatively lower torque ripple (20%-40%), which is lower than those of 6s10p and 12s8p SRMs. It is also shown that designs close to the Pareto fronts naturally have relatively low torque ripple compared with other regions in the design space. Further reduction of the torque ripple needs to include the turnon angle and turn-off angle (or dwell angle) as independent variables, and involve sophisticated control methods in the optimization process. Commonly used methods for reducing the torque ripple include current profiling [29], the use of an increased number of phase [30], etc. It may be noted that these methods are also applicable to the machine topologies studied in this paper.

#### C. Radial Force and Consideration of Mechanical Aspects

Compared with the 6s10p and 12s8p SRMs, the 12s26p topology needs additional rotor frame to hold the segments and provide enough stiffness to prevent unacceptable deformations caused by radial forces. The radial magnetic force density distributions of M-1, M-2 and M-3 along the rotor circumferential are calculated from the airgap flux density waveforms and compared at the instant of time when the peak radial force occurs, as shown in Fig. 12. It can be seen that the 12s26p design has the lowest peak radial force density, which may be attributed to the large number of rotor poles and short magnetic flux paths. The relatively low radial force density is expected to simplify the mechanical design of the rotor frame.



Fig. 12. Radial force density distributions in Nm/mm<sup>2</sup> of M-1, M-2 and M-3.

## D. Power Factor and VA Rating

Both the voltage and current waveforms of SRMs are nonsinusoidal, so the power factor has to be calculated using the definition for non-sinusoidal systems, which is a figure of merit that measures how efficiently energy is transmitted and always lies between 0 and 1 [31]. Such a definition is consistent with the power factor used in sinusoidal systems and thus suitable for the comparison between SRMs and conventional ac machines based on general power or torque equations [32]. The power factor is less straightforward than the VA rating in sizing converters for SRMs [18]. The converter VA rating, therefore, instead of the power factor, is calculated for this study.

The converter VA rating at the rated operating point is plotted against the saliency ratio, as shown in Fig. 13. It is seen that all the manifestations of the 12s8p SRM have a higher saliency ratio than the other two topologies. It is also noted that, for each topology, there is an inverse correlation between the converter VA rating and the saliency ratio. In addition, the 12s26p and 6s10p SRMs generally have lower saliency ratio and higher VA rating requirement than 12s8p designs.



Fig. 13. The converter VA rating versus the saliency ratio for all evaluated designs. For a specific SRM topology, the converter VA rating approximately varies inversely with the saliency ratio.

### E. Experimental Results

The current work expands on a previously reported experimental study for a prototype SRM with a 12 slot stator and a modular/segmented rotor with 26 poles [20] with new insights and results provided, and provides additional results and new technical insights. This prototype SRM was employed both for establishing an experimental validation basis for the



Fig. 14. Segmented SRM prototype: (a) stator with coils, (b) rotor with module/segment holder, (c) comparison between laminations of the selected optimal design and the prototype. The rotor laminations include dovetails and bridges to simplify the manufacturing process.

electromagnetic field FEA of the type employed for the study of hundreds of candidate designs, as well as an initial reference for the optimization and for the ranges of the design space considered.

The stator and rotor of the prototype SRM are shown in Fig. 14 in a new perspective, together with a cross section of the laminated core, clearly illustrating the rotor construction with ferromagnetic independent modules. The rotor laminations for the actual prototype, which included a dovetail profile, were produced through a wire cutting process with inter-module bridges, which were then machined off before attaching the core modules to a frame made of non-magnetic stainless steel. The total outer diameter and airgap length of the prototype and of the previously selected design M1 are the same with the values listed in I. The stack length of the prototype machine is 40mm and the total axial length is 102mm taking into account the end coils. The lamination steel material used is M27-29G for both the stator and rotor. The stator coils were hand wound with an equivalent slot fill factor of 0.33.

The optimization study, previously discussed in the paper, included FEA of hundreds of SRMs and yielded a Pareto font, i.e. a collection of best compromise designs that is representative of the tradeoffs between loss and mass. The location of the prototype, operating at 18Nm and 600rpm, in the loss-mass plane shown in Fig. 9. is denoted by the largest star. For all practical engineering purposes, especially when considering the inherent differences arising due to manufacturing variations, combined computational errors and measurement uncertainties, the prototype lies on the Pareto front in a region of relatively higher loss and lower mass.

The inductances at various rotor positions shown in Fig. 15 were obtained by measuring the time constant with phase A winding connected in series with an external resistor and supplied by a signal generator. A small value 1.25 mH is considered as the end winding leakage inductance and subtracted from the measured waveform. It is shown that the unsaturated inductance agrees well with that predicted from 2D FEA.



Fig. 15. Comparison of simulated and measured inductance waveforms.

The static torque with only one phase excited by different dc currents was measured at various rotor positions. The measured peak static torque at different currents is plotted in Fig. 16, and shows good agreement with the 2D FFA predictions.



Fig. 16. Comparison of simulated and measured peak values of static torque at different phase currents.

The loss breakdown at 13 Nm and various speeds is shown in Fig. 17. With the increase of the rotor speed, the core losses increase accordingly but the copper loss is the same. The difference between the FEA predicted and measured losses is mainly caused by the mechanical loss, which is not considered in the prediction.

## V. CONCLUSION

The paper introduces a design method for switched reluctance machines (SRMs) that combines a differential evolutionbased multi-objective optimization technique with fast 2D FEA based on pre-determined current profile estimations, which consider the power electronic drive controls and result in a substantial reduction of the computational effort, as compared with conventional approaches. The new method



Fig. 17. Comparison of simulated and measured losses at 13 Nm and various speeds.

is supporting another contribution of the paper, which is represented by systematic optimal design comparative studies for three outer-rotor motor topologies for in-wheel directdrive applications. The two objectives considered are mass and losses and the hundreds of SRMs analyzed yield a Pareto front of best compromise designs.

The studies reported include an innovative SRM topology with a modular and segmented rotor for which a prototype was built and tested. The optimization yielded a comprehensive Pareto front that includes the best compromise designs for which improvement can be achieved only by trading off the two objectives of mass and loss. The Pareto spans a relatively large performance space with max to min ranges of approx. 1.25 and 1.7 for losses and mass, respectively. For all practical engineering purposes, the prototype SRM discussed in the paper lays on the Pareto in the more cost competitive higher-loss lower-mass region and additionally provides useful technical insights.

It is also shown that modular and segmented rotor SRMs are superior, in terms of specific torque and efficiency, to the conventional configuration motors considered. Furthermore, the large scale studies with hundreds of candidate designs indicate that SRMs with higher number of rotor poles than stator teeth have higher converter volt-ampere rating.

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