

Overview of Flywheel Systems for Renewable Energy Storage with a Design Study for High-speed Axial-flux Permanent-magnet Machines

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Abstract—Flywheel energy storage is considered in this paper for grid integration of renewable energy sources due to its inherent advantages of fast response, long cycle life and flexibility in providing ancillary services to the grid, such as frequency regulation, voltage support, etc. The fundamentals of the technology and recent developments are reviewed, firstly with an emphasis on the design considerations and performance metrics. Then the progress and development trends in electric motor/generators employed in flywheel energy storage systems (FESS) are summarized, showing the potential of axial-flux permanent-magnet (AFPM) machines in such applications. Design examples of high-speed AFPM machines are provided and evaluated in terms of specific power, efficiency, and open-circuit losses in order to validate their suitability in FESS.

Index Terms—Axial-flux, flywheel energy storage system, motor/generator, permanent-magnet.

I. INTRODUCTION

Recent technological developments have spawned the growth of renewable energy resources, such as solar and wind power. The intermittent nature of these resources may introduce issues with system stability, reliability and power quality. Storing power from these intermittent sources with energy storage systems partially decouples the energy generation from demand and is thus considered as an effective approach to addressing problems introduced by the penetration of renewable energies [1], [2]. Interests in energy storage have seen rapid growth recently and the renewable energy industry is expected to generate a larger proportion of the overall energy consumption in the near future.

Energy can be stored through various forms, such as ultra-capacitors, electrochemical batteries, kinetic flywheels, hydro-electric power or compressed air. Their comparison in terms of specific power, specific energy, cycle life, self-discharge rate and efficiency can be found, for example, in [3]. Compared with other energy storage methods, notably chemical batteries, the flywheel energy storage has much higher power density but lower energy density, longer life cycles and comparable efficiency, which is mostly attractive for short-term energy storage.

Flywheel energy storage systems (FESS) have been used in uninterrupted power supply (UPS) [4]–[6], brake energy recovery for racing cars [7], public transportation [8], off-highway vehicles [9], container cranes/straddle carriers [10], and grids [11]–[13]. They were also proposed to be used in the pulse power supply for electromagnetic launch systems [14]. Major manufacturers of FESS are tabulated in Table I, focusing on UPS, brake energy recovery and grid applications.

The FESS technology has been reviewed from various perspectives, such as the system level [18]–[21], mechanical aspects [22] and specific applications [23]. The latest technology progress focused on reducing the self-discharge and performing ancillary services, such as frequency regulation, voltage support, renewable energy integration and potential peak electric power shaving, showing the possibility of introducing FESS in grid applications [24].

II. FUNDAMENTALS OF FESS

A. Configurations and Principle of Operation

A typical FESS, as shown in Fig. 1, includes a flywheel rotor, an electric motor/generator and its associated drive, bearing systems, and a containment. The flywheel rotor is a moving mass that stores the kinetic energy. The machine and drive work in three modes of operation, i.e., charging, standby and discharging, and perform the energy conversion, as illustrated in Fig. 2. During the charging mode, the machine works as a motor and accelerates the flywheel, while in discharging mode, the machine serves as a generator and extracts the stored energy to supply the load.

Bearings are used to keep the flywheel rotor in place with very low friction. They can be mechanical, magnetic or hybrid. Active and/or passive magnetic bearings are usually employed to hold the flywheel during operation, ensuring a long life, reduced losses and low maintenance [25]. The high-temperature superconducting (HTS) type has also been proposed to levitate and rotate the flywheel [26]. Mechanical types may also be included to hold the flywheel while it is stationary or below operational speed. Additional catch bearings may be installed to

Table I
MAJOR MANUFACTURERS OF FESS AND THEIR APPLICATIONS

Manufacturer	Ratings	Applications
ABB	1,800-3,600 rpm, 100-1,500 kW	Renewable microgrid stabilization [11]
Active Power	Max. 10,000 rpm, 225 kW	UPS [4]
Beacon Power, LLC	Max. 16,000 rpm, 100 kW	Utility grid [13]
Calnetix Technologies, LLC	25,000-35,000 rpm, 125 kW	UPS [5]
Williams Hybrid Power	Max. 36,000-45,000 rpm, 150-180 kW	Brake energy recovery for vehicles [7]
Kinetic Traction Systems	Max. 36,000 rpm, 250-400 kVA	Brake energy recovery, UPS and grid [15]
PowerThru	-	UPS [6]
PUNCH Flybrid	Max. 60,000 rpm, 60 kW	Brake energy recovery for vehicles [9]
Ricardo PLC	Max. 44,000 rpm, 100 kW	Brake energy recovery for vehicles [16]
Temporal Power	-	Utility grid [17]

provide a fail-safe system. The containment not only provides an environment with low aerodynamic drag, but also shields the fragments in the event of rotor failures.

B. Sizing Procedure for Flywheel Rotors

Flywheel rotors are built as solid or hollow cylinders. The maximum kinetic energy stored in the flywheel E_k is:

$$E_k = \frac{1}{2} J \omega^2, \quad (1)$$

where ω_{max} is the maximum angular velocity, J is the moment of inertia, which is a function of the mass and shape of the rotor, and for hollow cylinders, it can be expressed as:

$$J = \frac{1}{2} m (r_o^2 + r_i^2) = \frac{\rho \pi h}{2} (r_o^4 - r_i^4), \quad (2)$$

where m is the flywheel rotor mass and ρ the mass density, r_o and r_i are the outer radius and inner radius of a hollow cylinder flywheel, respectively, h is the thickness of the flywheel rotor in axial direction. The useful energy of a flywheel within a speed range of minimum speed ω_{min} and maximum speed ω_{max} can be obtained by:

$$E_{keff} = \frac{1}{2} J (\omega_{max}^2 - \omega_{min}^2) = \frac{1}{2} J \omega_{max}^2 \left(1 - \frac{\omega_{min}^2}{\omega_{max}^2} \right), \quad (3)$$

The ratio $\omega_{min}/\omega_{max}$ depends on the voltage variation and maximum torque for a given power rating. The peak torque occurs at the lowest speed in discharging mode, as shown in Fig. 2. A typical value for $\omega_{min}/\omega_{max}$ is 0.5, in which case, 75% of the total stored energy can be extracted from the flywheel. The selection of this value also has an impact on the life cycle [27].

The outer radius is limited by the yield stress of the material σ_y , external stress σ_{sh} introduced by the shrink-fit between the flywheel rotor and shaft, Poisson's ratio ν and the maximum rotating speed of the flywheel ω_{max} :

$$r_o < \sqrt{\frac{4(\sigma_y - \sigma_{sh})}{(3 + \nu)\rho\omega_{max}^2} - \frac{1 - \nu}{3 + \nu} r_i^2}, \quad (4)$$

The thickness in the axial direction can then be estimated by:

$$h = \frac{4E_k}{\rho\pi\omega_{max}^2 (r_o^4 - r_i^4)}. \quad (5)$$

Based on (4) and (5), the maximum specific energy is:

$$\frac{E_k}{m} = K \frac{\sigma_y}{\rho}, \quad (6)$$

where K is the shape factor of the hollow cylinder flywheel with isotropic material, such as steel:

$$K = \frac{\left(1 - \frac{\sigma_{sh}}{\sigma_y} \right) \left[\left(\frac{r_i}{r_o} \right)^2 + 1 \right]}{\left[(1 - \nu) \left(\frac{r_i}{r_o} \right)^2 + (3 + \nu) \right]}. \quad (7)$$

The shape factor K is a measurement of material utilization and depends on the flywheel geometry, as summarized in [28]. Considering ease of manufacturing and assembling, conventional flywheel rotors are hollow cylinders with central holes to install the shaft, which are used to couple the electric motor/generator.

Equation (6) indicates that the specific energy (energy per mass unit) and energy density (energy per volume unit) of the flywheel are dependent on its shape, expressed by the shape factor K , and the yield stress σ_y . By contrast, the power rating depends on the motor/generator characteristics. This means the energy and power rating can be sized independently, depending on the application requirements. This flexibility is a particularly advantageous feature of flywheel technology.

To achieve high-specific-energy flywheels, strong materials with low mass densities are needed. Typical materials used in flywheel rotors are listed in Table II based on data from [28]. The fatigue strength for a cycle life of 10^7 cycles σ_f instead of the yield strength is used to give more practical estimations about the energy density and specific energy. The calculation of E_k/m and E_k/V for hollow cylindrical flywheels made of metal uses $K = 0.305$ and $K = 0.500$ is used for flywheels made of filamentary composites.

C. Performance Metrics

Uniform parameters and evaluation methods have been defined by the Pacific Northwest National Laboratory (PNNL) and Sandia national Laboratories (SNL) to serve as the basis to compare the performance of different energy storage systems. The definitions are applicable to various energy storage methods but not all of them are of special interest to a specific storage method. In this section, only metrics essential to FESS

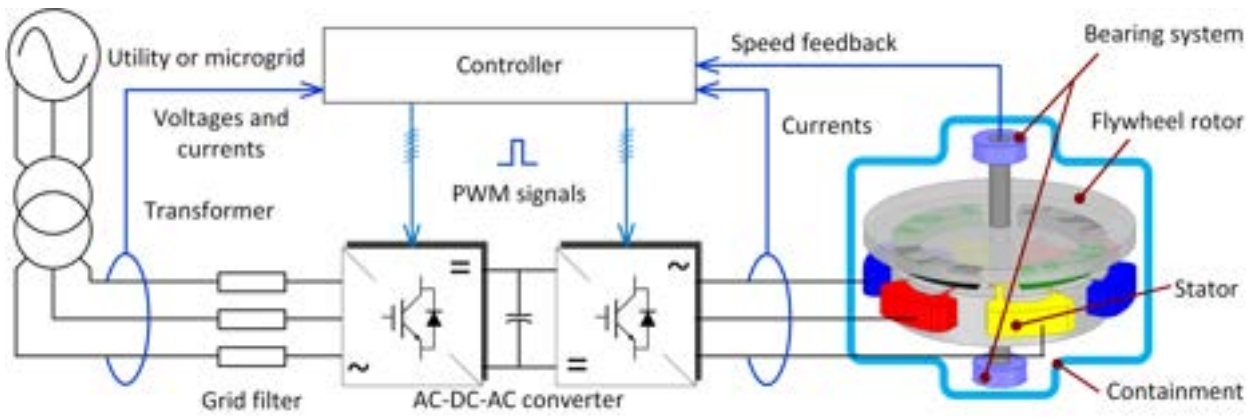


Figure 1. A typical FESS with a solid flywheel rotor. A transparent view of the rotor back iron is employed in order to show PMs and stator coils.

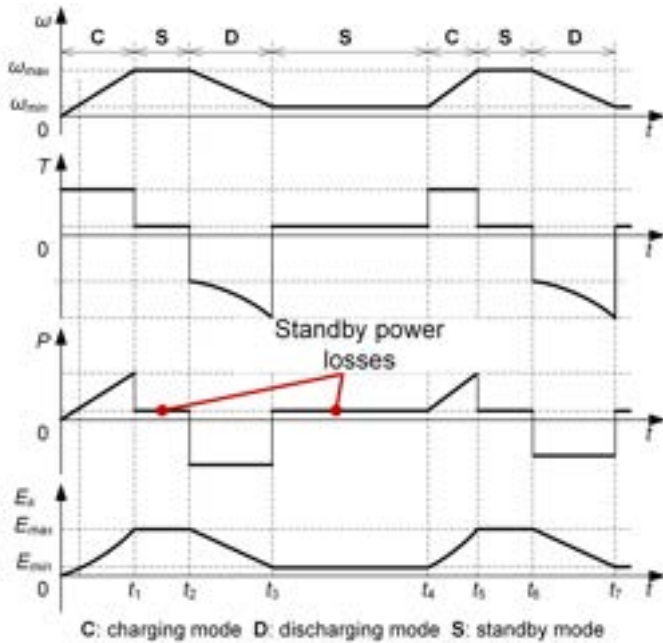


Figure 2. Typical operating cycles for FESS. The power rating is limited by the lowest speed in discharging mode, where the maximum torque occurs. The standby power losses are shown disproportionately for illustration purposes.

Table II
FLYWHEEL MATERIAL CHARACTERISTICS.

Material	ρ (kg/m ³)	σ_y (MPa)	σ_f (MPa)	E_k/V (kWh/m ³)	E_k/m (Wh/kg)
Steel - wrought	7,800	950	550	46.6	6.0
Steel - maraging	8,000	2,337	765	64.8	8.1
Titanium	4,500	1,186	662	56.1	12.4
Fiber - glass	2,000	1,100	220	30.0	15.0
Fiber - aramid	1,400	1,400	700	97.0	69.0
Fiber - Carbon	1,550	2,000	1,600	222.0	143.0

are presented. Table III lists the statistical results of published FESS in terms of these performance. The definitions of depth of discharge, round-trip efficiency and standby power losses are presented below. The details related to other performance metrics can be found in [29].

The depth of discharge is the percentage of flywheel energy capacity that has been discharged, expressed as a percentage of

Table III
PUBLISHED METRICS OF FESS. STATISTICAL RESULTS FROM MULTIPLE SOURCES.

Metric	Value
Power rating (MW)	0.001-10
Specific energy (Wh/kg)	5-200
Specific power (W/kg)	400-30,000
Energy density (kWh/m ³)	0.25-424
Power density (kW/m ³)	40-2,000
Round-trip efficiency (%)	70-96
Calendar life (year)	15-20
Cycle life (cycles)	10,000-100,000
Self-discharge rate (%/day)	24-100

the maximum capacity. The depth of discharge of flywheels is up to the output power and the maximum current of the power converter.

The round-trip efficiency is expressed as a percentage of the useful output energy with respect to the input energy over one duty cycle under normal conditions. The time period from t_3 to t_7 in Fig. 2 is a typical operating cycle. Round-trip efficiency is a pivotal design factor especially for long-term FESS. Nowadays, the round-trip efficiency of FESS can reach 80%-95%. The key metrics of FESS listed in Table III are based on data compiled from [4]–[7], [9], [11], [13], [15]–[18].

The standby power losses are loss components that gradually reduce the stored energy in the standby mode of operation. The standby power losses depend on the design of flywheels and are usually caused by friction, aerodynamic drag and open-circuit motor/generator losses that slow down the rotor. To reduce the standby power losses, vacuum containment and magnetic bearings are usually employed [20], [21]. The standby losses are designed to be very low, typically less than 25 W/kWh of the stored energy and in the range of 1-2% of the rated output power.

III. ELECTRIC MACHINES FOR FESS

A. Machine Topologies

PM brushless machines and squirrel-cage induction machines of the radial-flux type have been widely used in FESS. Radial-flux and transverse-flux homopolar induction machines have drawn much attention during the past two decades considering

their low-standby-loss nature and the ease of integrating the electric machine rotor with the flywheel [30]–[32]. However, the torque/power density of this type is relatively low compared with induction machines and PM brushless machines [33]. Other machines, such as synchronous reluctance machines, and bearingless versions of PM brushless machines and induction machines have also been proposed, yet experimental demonstrations of the feasibility are still rare.

B. Research and Development Trends

The research in electric machines for FESS mainly focuses on the reduction of standby power losses. The use of magnetic or HTS bearings and installing the flywheel in low-pressure containments are effective ways to achieve the goal. Flywheel energy storage tends to use various active/passive magnetic and HTS bearings to reduce the losses caused by friction as well as extend the lifetime for maintenance-free operation. Retractable configurations, i.e., adjustable airgaps [34], [35], and slotless or coreless structures [36] have also been used to reduce the standby power losses. The heat dissipation and thermal analysis of electric machines are of significance if the motor/generators are included in the low-pressure containments considering the very low convective heat transfer in such conditions.

C. AFPM Machines

AFPM brushless machines have also been proposed for FESS. An AFPM machine in a vertical arrangement with two stators and one central rotor has been presented to improve the round-trip efficiency by making full use of the axial forces instead of active/passive bearings in [37]. The central rotor serves as the flywheel of the integrated system and the magnetic attractions between the rotor and stators were controlled appropriately to counteract the rotor gravity. A flywheel system with an axial-flux motor/generator whose airgap can be adjusted dynamically to reduce the standby power losses during idle periods has also been proposed [35]. A micro-flywheel energy storage with an AFPM machine and HTS bearing was fabricated and tested in [38]. The disk-type aluminum rotor with high moment of inertia was used as the flywheel rotor and the maximum speed reached 51,000 rpm.

IV. DESIGN STUDY OF HIGH-SPEED AFPM MACHINES FOR FESS

In this section, two main topologies, i.e., the conventional single-sided AFPM machine with stator and rotor cores and the coreless structure with two rotors and a central stator, as illustrated in Fig. 3, are evaluated by finite element analysis (FEA) to show their suitability for FESS applications in terms of specific power, efficiency and open-circuit losses. Both 3-phase and 2-phase windings can be employed in the AFPM machines under study. The coreless design example adopts the 2-phase wave winding in order to show the enhanced fault-tolerant capability due to the magnetic decoupling between the two phases.

The proposed motor/generator designs are modular low-power high-speed units. They have the same power rating

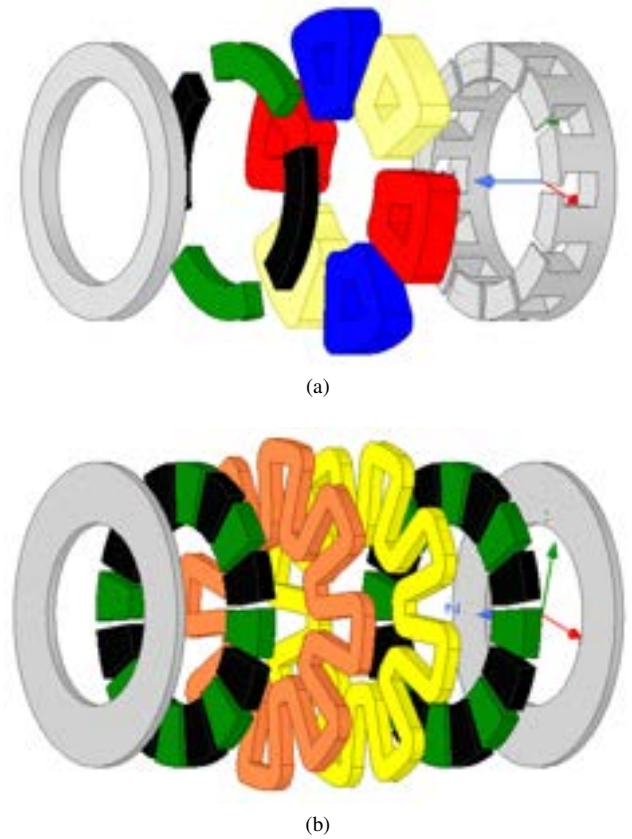


Figure 3. Two typical AFPM machine topologies, (a) with stator core, (b) without stator core. Concentrated or wave-type windings may be used to reduce the length of end winding and associated copper losses, as well as for the ease of manufacturing. Solid conductors are depicted for illustration, and they would be made of fine wire or Litz wire to minimize the high-frequency AC losses.

17.5 hp and will run between 25,000 rpm and 50,000 rpm, corresponding to a maximum depth of discharge 0.5. The same envelope dimensions, i.e., total outer diameter = 200 mm and total axial length = 50 mm, are used for both the designs with and without stator core. The magnet grade is NdFeB N30 and the stator core is made of lamination steel M15-29G.

For the AFPM machine with core, the fundamental frequency at very high speed operation and number of poles are limited by the core losses, which are approximately proportional to the square of fundamental frequency. By eliminating the stator core and associated core losses, the coreless design may employ a higher number of poles. A parametric study is carried out to show the influence of number of poles on the motor/generator performance. The current density is adjusted accordingly to achieve the target torque 5 Nm at 25,000 rpm. The motor/generator can operate up to 50,000 rpm but the torque is reduced to 2.5 Nm to maintain constant output power.

As shown in Fig. 4, the coreless machine designs can achieve a specific power output of around 6 kW/kg, regardless of the number of poles from 4 to 10, while the design with stator core has a much lower value due to the required large core volume and mass. Furthermore, the applied current density reduces with the increase in the number of poles for coreless machines. This is caused by the relatively low torque capability of machines

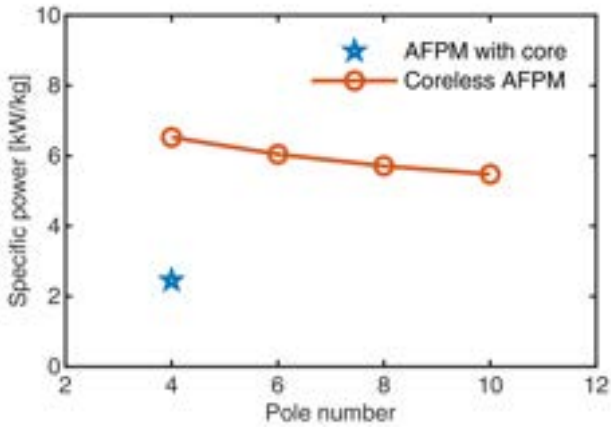


Figure 4. Specific power of AFPM machine design examples with and without stator core. The pole number of the design with stator core is mainly limited by the core losses at high rated frequencies. In contrast, the coreless design may have more poles due to the elimination of core losses.

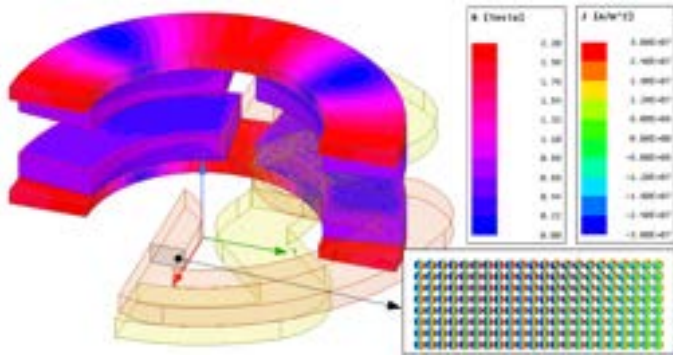


Figure 5. Flux density and instantaneous current density distribution for an example 4-pole coreless design using multi-strand conductors at 25,000 rpm. The high induced current densities indicate that Litz wire may need to be used to mitigate the high frequency conductor losses.

with a low number of poles for a small ratio of total axial length to total diameter [39].

It may be noted that coreless machines tend to feature high conductor AC losses, due to eddy currents induced by the time-dependent variations of the airgap magnetic field, and therefore would need to be designed with fine multi-strand conductors or Litz wire. For the example design based on multi-strand conductors shown in Fig. 5, the induced instantaneous current density is more than twice the applied current density at 25,000 rpm, indicating that the use of Litz wire may be necessary in this case.

The efficiency of the designed electric machines in charging/discharging mode is shown in Fig. 6. It may be observed that the efficiency is almost invariant with the number of poles for the operation at 25,000 rpm, while at 50,000 rpm, the efficiency drops sharply with the increase of pole number, indicating that either a lower rotor polarity, or a winding design with Litz wire may be the right choice.

It is worth noting that in order to operate AFPM machines with relatively large pole numbers at very high speeds, it is

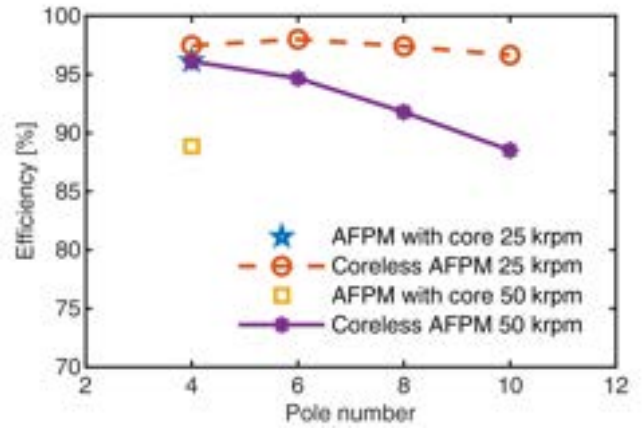


Figure 6. Efficiency of AFPM machine design examples with and without stator core at 25,000 rpm and 50,000 rpm.

necessary to use wide-bandgap (WBG) switching devices to enable higher fundamental frequency as well as improve the system efficiency, such as silicon carbide (SiC) and gallium nitride (GaN) metal oxide semiconductor field effect transistors (MOSFETs). Inverters with all WBG devices or hybrid switch converters can be employed to drive the proposed low-power high-speed units.

FEA results indicate that designs with a low number of poles are preferred in terms of open-circuit loss. In order to take advantage of the high torque per ampere provided by higher polarity designs, the open circuit loss can be mitigated by increasing the airgap length in standby mode.

The round-trip efficiency is closely related to both the efficiency in charging/discharging mode and power losses in standby mode. In short-term energy storage applications, the efficiency in charging/discharging mode may be more important. For long-term flywheel energy storage, the standby mode may last a long period of time and the standby power losses become the dominating loss component in a whole round trip.

Based on the calculation results of the design examples, it can be found that AFPM machines, especially those with stator cores, are subject to the constraints on the fundamental frequency. Low number of poles are favored to reduce the open-circuit loss. In the case of coreless machines, relatively larger pole numbers provide higher specific power at the same current density level and higher efficiency in the designed charging/discharging speed range. Coreless designs may need to use Litz wire in order to minimize the additional conductor losses at high frequency. It should be noted that the current density in conductors and heat dissipation of stator windings may bring about additional challenges in designing high-speed AFPM machines for FESS applications.

V. CONCLUSION

This paper reviews the fundamentals and recent developments of flywheel energy storage technology, with an emphasis on applications in microgrid and utility grid for renewable energy integration. To achieve high energy density/specific

energy, composite materials with high tensile strength and low mass density are becoming increasingly popular in constructing flywheel rotors, enabling higher rotor speeds and larger rotor diameters.

High-speed AFPM machines are evaluated in terms of power density/specific power, efficiency, and open-circuit power losses at high rotating speeds, showing their feasibility in FESS with high energy density/specific energy. The adjustable air-gap length of AFPM machines may further benefit the self-discharge reduction in the standby mode. In addition, there is a higher potential to integrate the rotor of axial-flux PM motor/generator with the flywheel rotor due to its disk-like shape. The design study conducted in this paper opens up an opportunity for AFPM machines in the grid integration of renewable energy sources.

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REFERENCES

- [1] V. A. Boicea, "Energy storage technologies: The past and the present," *Proceedings of the IEEE*, vol. 102, no. 11, pp. 1777–1794, Nov 2014.
- [2] S. Vazquez, S. M. Lukic, E. Galvan, L. G. Franquelo, and J. M. Carrasco, "Energy storage systems for transport and grid applications," *IEEE Transactions on Industrial Electronics*, vol. 57, no. 12, pp. 3881–3895, Dec 2010.
- [3] F. Blaabjerg and D. M. Ionel, *Renewable Energy Devices and Systems with Simulations in MATLAB® and ANSYS®*. CRC Press, May 2017.
- [4] ActivePower. [Online]. Available: <http://www.activepower.com/en-GB/downloads>
- [5] Calnetix Technologies, LLC. [Online]. Available: <https://www.calnetix.com/powerflux-active-magnetic-bearings>
- [6] PowerThru. [Online]. Available: <http://www.power-thru.com/>
- [7] J. G. R. Hansen and D. U. O’Kain, "An assessment of flywheel high power energy storage technology for hybrid vehicles," Tech. Rep., Dec. 2011, ORNL/TM-2010/280.
- [8] M. Andriollo, F. Graziottin, and A. Tortella, "Contact-less electromagnetic recharging system for heavy-duty bus flywheel storage," in *2015 International Conference on Renewable Energy Research and Applications (ICRERA)*, Nov 2015, pp. 232–237.
- [9] PUNCH Flybrid. [Online]. Available: <https://punchflybrid.com/applications/>
- [10] M. M. Flynn, P. McMullen, and O. Solis, "High-speed flywheel and motor drive operation for energy recovery in a mobile gantry crane," in *APEC 07 - Twenty-Second Annual IEEE Applied Power Electronics Conference and Exposition*, Feb 2007, pp. 1151–1157.
- [11] ABB, "Powerstore - renewable microgrid stabilization," Nov. 2017.
- [12] S. Sanders, M. Senesky, M. He, and E. Chiao, "Low-cost flywheel energy storage demonstration," Tech. Rep., 2015. Publication number: CEC-500-2015-089.
- [13] Beacon Power, LLC. [Online]. Available: <https://beaconpower.com/>
- [14] M. R. Doyle, D. J. Samuel, T. Conway, and R. R. Klimowski, "Electromagnetic aircraft launch system-EMALS," *IEEE Transactions on Magnetics*, vol. 31, no. 1, pp. 528–533, Jan 1995.
- [15] Kinetic Traction Systems, Inc. [Online]. Available: <https://kinetic-traction.com/flywheel-energy-storage-applications/>
- [16] Ricardo PLC. [Online]. Available: <https://ricardo.com/news-and-media/news-and-press/flybus-to-start-testing-first-flywheel-hybrid-bus>
- [17] Temporal power. [Online]. Available: <http://temporalpower.ca/>
- [18] S. Sabihuddin, A. Kiprakis, and M. Mueller, "A numerical and graphical review of energy storage technologies," *Energies*, vol. 8, no. 1, pp. 172–216, Dec 2014.
- [19] M. E. Amiryar and K. R. Pullen, "A review of flywheel energy storage system technologies and their applications," *Applied Sciences*, vol. 7, no. 3, pp. 1–21, Mar. 2017.
- [20] P. Yulong, A. Cavagnino, S. Vaschetto, Chai Feng, and A. Tenconi, "Flywheel energy storage systems for power systems application," in *2017 6th International Conference on Clean Electrical Power (ICCEP)*, June 2017, pp. 492–501.
- [21] S. Mousavi G, F. Faraji, A. Majazi, and K. Al-Haddad, "A comprehensive review of flywheel energy storage system technology," *Renewable and Sustainable Energy Reviews*, vol. 67, pp. 477 – 490, 2017.
- [22] E. Dragoni, "Mechanical design of flywheels for energy storage: A review with state-of-the-art developments," *Proceedings of the Institution of Mechanical Engineers, Part L: Journal of Materials: Design and Applications*, vol. 233, no. 5, pp. 995–1004, 2019.
- [23] M. Hedlund, J. Lundin, J. De Santiago, J. Abrahamsson, and H. Bernhoff, "Flywheel energy storage for automotive applications," *Energies*, vol. 8, no. 10, pp. 10636–10663, 2015.
- [24] F. Goris and E. L. Severson, "A review of flywheel energy storage systems for grid application," in *IECON 2018 - 44th Annual Conference of the IEEE Industrial Electronics Society*, Oct 2018, pp. 1633–1639.
- [25] J. Itoh, T. Masuda, D. Sato, T. Nagano, T. Suzuki, and N. Yamada, "Development of magnetic assist system in flywheel energy storage system for power load-leveling," in *2016 IEEE International Conference on Renewable Energy Research and Applications (ICRERA)*, Nov 2016, pp. 198–203.
- [26] M. Strasik, J. R. Hull, J. A. Mittleider, J. F. Gonder, P. E. Johnson, and K. E. McCrary, *et al.*, "An overview of boeing flywheel energy storage systems with high-temperature superconducting bearings," *Superconductor Science and Technology*, vol. 23, no. 3, p. 034021, Feb 2010.
- [27] X. Li, B. Anvari, A. Palazzolo, Z. Wang, and H. Toliyat, "A utility-scale flywheel energy storage system with a shaftless, hubless, high-strength steel rotor," *IEEE Transactions on Industrial Electronics*, vol. 65, no. 8, pp. 6667–6675, Aug 2018.
- [28] F. Thoolen, "Development of an advanced high speed flywheel energy storage system," Ph.D. dissertation, Technische Universiteit Eindhoven, Eindhoven, January 1993.
- [29] D. R. Conover, S. R. Ferreira, A. J. Crawford, D. A. Schoenwald, J. Fuller, and D. M. R. S. N. Gourisetti, *et al.*, "Protocol for uniformly measuring and expressing the performance," Tech. Rep., Apr. 2016. PNNL-22010 Rev 2 / SAND2016-3078 R.
- [30] P. Tsao, M. Senesky, and S. R. Sanders, "An integrated flywheel energy storage system with homopolar inductor motor/generator and high-frequency drive," *IEEE Transactions on Industry Applications*, vol. 39, no. 6, pp. 1710–1725, Nov 2003.
- [31] E. Severson, R. Nilssen, T. Undeland, and N. Mohan, "Magnetic equivalent circuit modeling of the ac homopolar machine for flywheel energy storage," *IEEE Transactions on Energy Conversion*, vol. 30, no. 4, pp. 1670–1678, Dec 2015.
- [32] M. Andriollo, F. Bortot, and A. Tortella, "Disc-type pm machine for the electromagnetic conversion/suspension of a flywheel system," in *2015 International Conference on Renewable Energy Research and Applications (ICRERA)*, Nov 2015, pp. 739–744.
- [33] C. Ye, J. Yang, F. Xiong, and Z. Q. Zhu, "Relationship between homopolar inductor machine and wound-field synchronous machine," *IEEE Transactions on Industrial Electronics*, 2019, doi: 10.1109/TIE.2019.2898577.
- [34] M. Garcia-Gracia, M. A. Cova, M. T. Villen, and A. Uson, "Novel modular and retractable permanent magnet motor/generator for flywheel applications with reduced iron losses in stand-by mode," *IET Renewable Power Generation*, vol. 8, no. 5, pp. 551–557, July 2014.
- [35] J. G. Bitterly and S. E. Bitterly, "Flywheel based energy storage system," U.S. Patent 5 614 777, Mar. 1997.
- [36] S. R. Holm, "Modeling and optimization of a permanent magnet machine in a flywheel," Ph.D. dissertation, Technische Universiteit Delft, Delft, Nov 2003.
- [37] T. D. Nguyen, K. Tseng, S. Zhang, and H. T. Nguyen, "A novel axial flux permanent-magnet machine for flywheel energy storage system: Design and analysis," *IEEE Transactions on Industrial Electronics*, vol. 58, no. 9, pp. 3784–3794, Sep. 2011.
- [38] J. eun Yi, K. W. Lee, B. Kim, J. Ko, S. Jeong, and M. D. Noh, *et al.*, "Micro-flywheel energy storage system with axial flux machine," in *2007 IEEE/ASME international conference on advanced intelligent mechatronics*, Sep. 2007, pp. 1–6.
- [39] A. Cavagnino, M. Lazzari, F. Profumo, and A. Tenconi, "A comparison between the axial flux and the radial flux structures for PM synchronous motors," *IEEE Transactions on Industry Applications*, vol. 38, no. 6, pp. 1517–1524, Nov 2002.